

Efros-Shklovskii Coulomb gap without disorder



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Glass



Solid but **not ordered**

Not equilibrated:

non-ergodic

Microscopic degrees of
freedom **localized**

Also works for electrons!

Quenched disorder

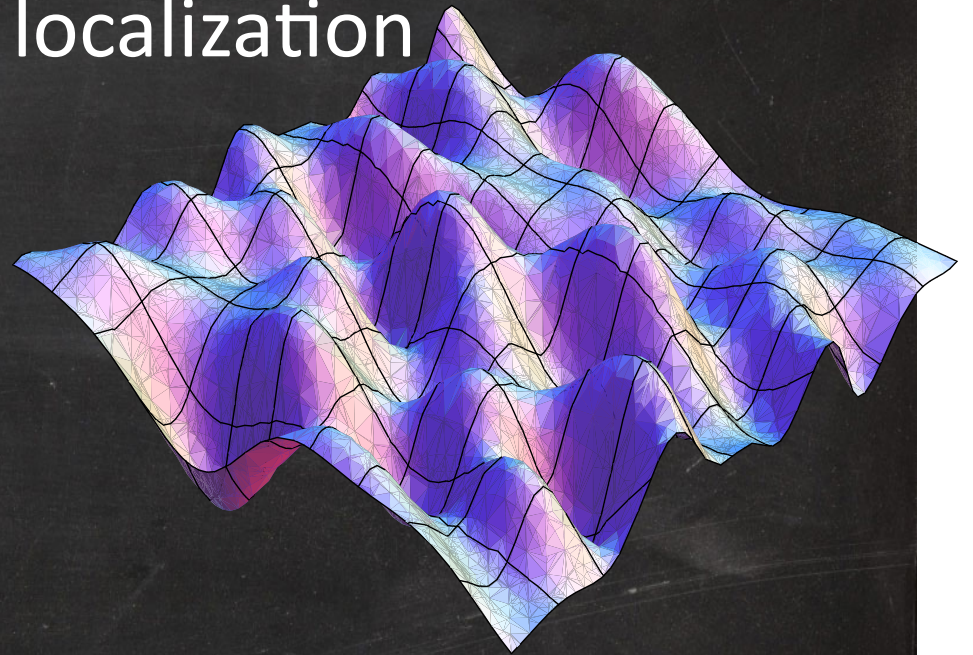
Parameters in Hamiltonian are **random**

No interactions: **Anderson** localization

$$H = \sum_i \mu_i n_i$$

Interactions: **Coulomb**

$$H_I = \frac{1}{2} \sum_{ij} \frac{V}{|r_{ij}|} (n_i - \bar{n}) (n_j - \bar{n})$$



Efros-Shklovskii gap (1)

Energy to remove or add a particle:

$$\epsilon_i = \mu_i + \frac{1}{2} \sum_{j \neq i} \frac{V}{|r_{ij}|} (n_j - \bar{n})$$

What is the **distribution** $g(\epsilon)$ of energies ϵ_i ?
(in the ground state)

Stability when electron moves from i to j:

$$\Delta E = \epsilon_j - \epsilon_i - \frac{V}{|r_{ij}|} > 0$$

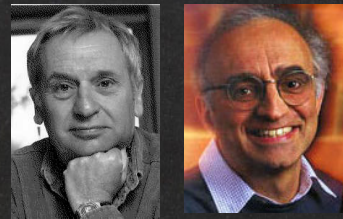
Efros-Shklovskii gap (2)

Distance between states close to Fermi level

$$|r_{ij}| > \frac{V}{\epsilon_j - \epsilon_i}$$

Stability sets upper **bound** for density of states

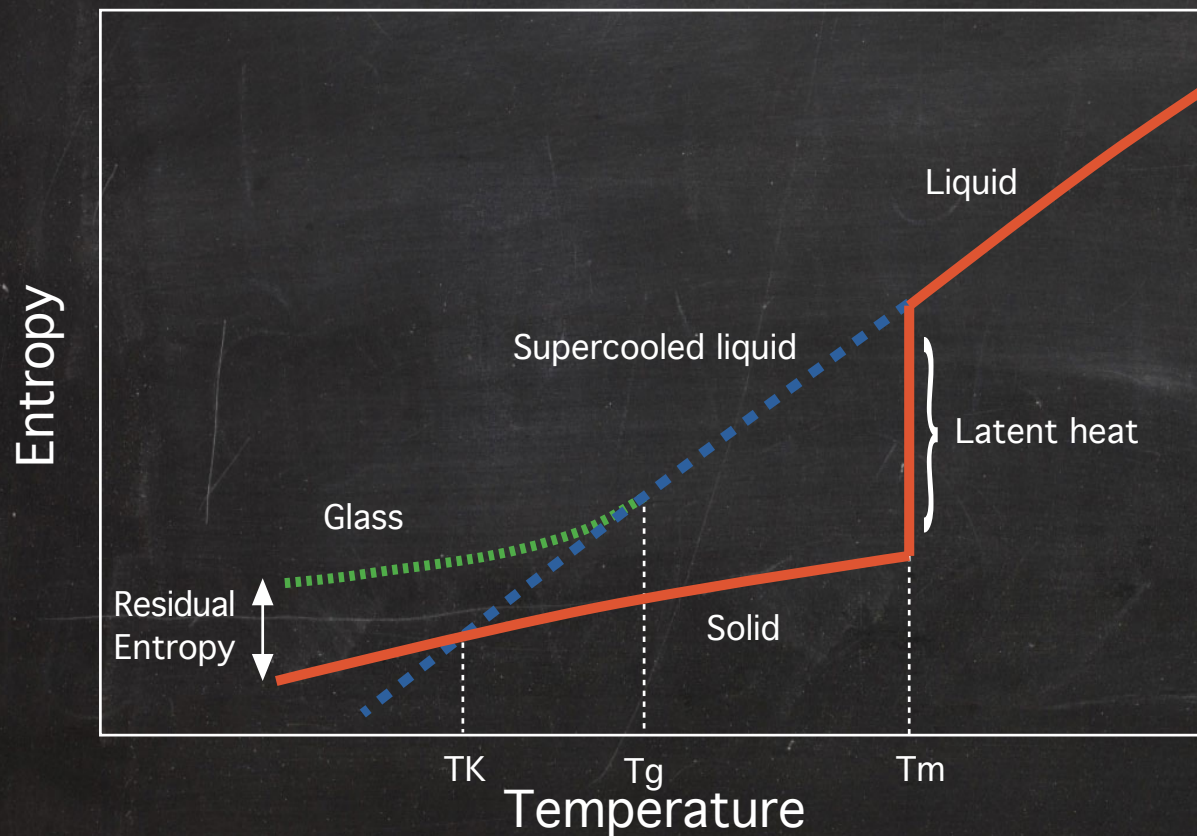
$$g(\epsilon) \leq \frac{d}{2\pi} |\epsilon|^{d-1}$$



Efros Shklovskii 1975

Wait.... glass?

Laws of physics (Hamiltonian) are **not** random!



Real glass = 🧐
supercool liquid

What about
electrons?

Disorderfree electron glasses

Quarter-filled triangular compound θ -RbZn

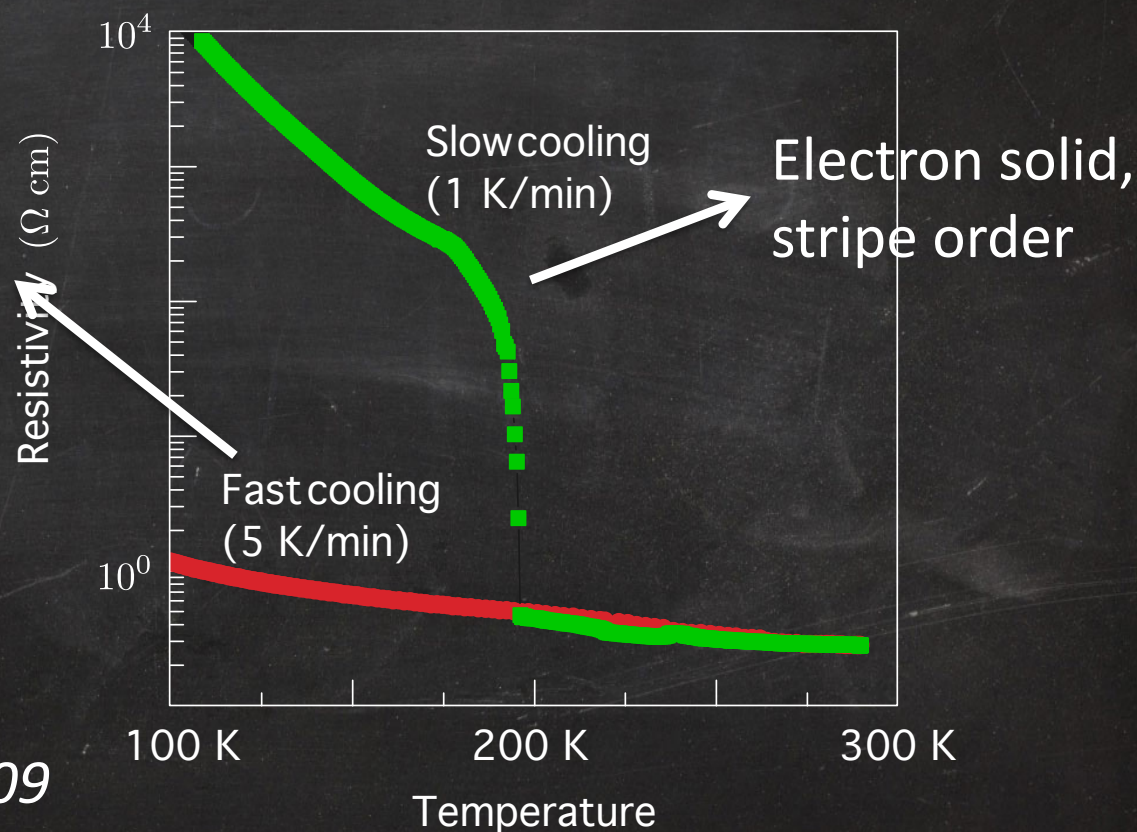


Supercool electron liquid!
Arrhenius Law dynamics

$$\tau \sim e^{\Delta/T}$$

Local charge correlations

Mahmoudian et al
APS March 2015 Q21.00009
arXiv:1412.4441



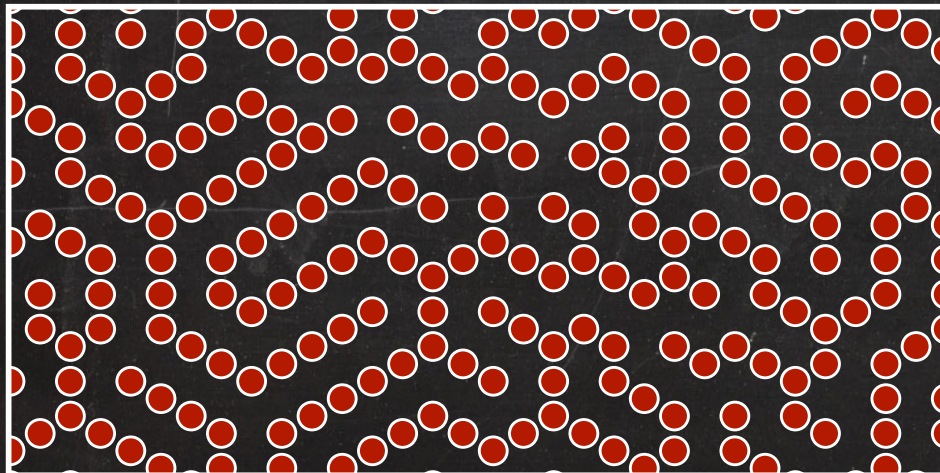
Kagawa, Nat Phys 2013

Metastable states

Glassiness: existence of **metastable states**

Metastability = electron move increases energy

$$\Delta E = \epsilon_j - \epsilon_i - \frac{V}{|r_{ij}|} > 0$$

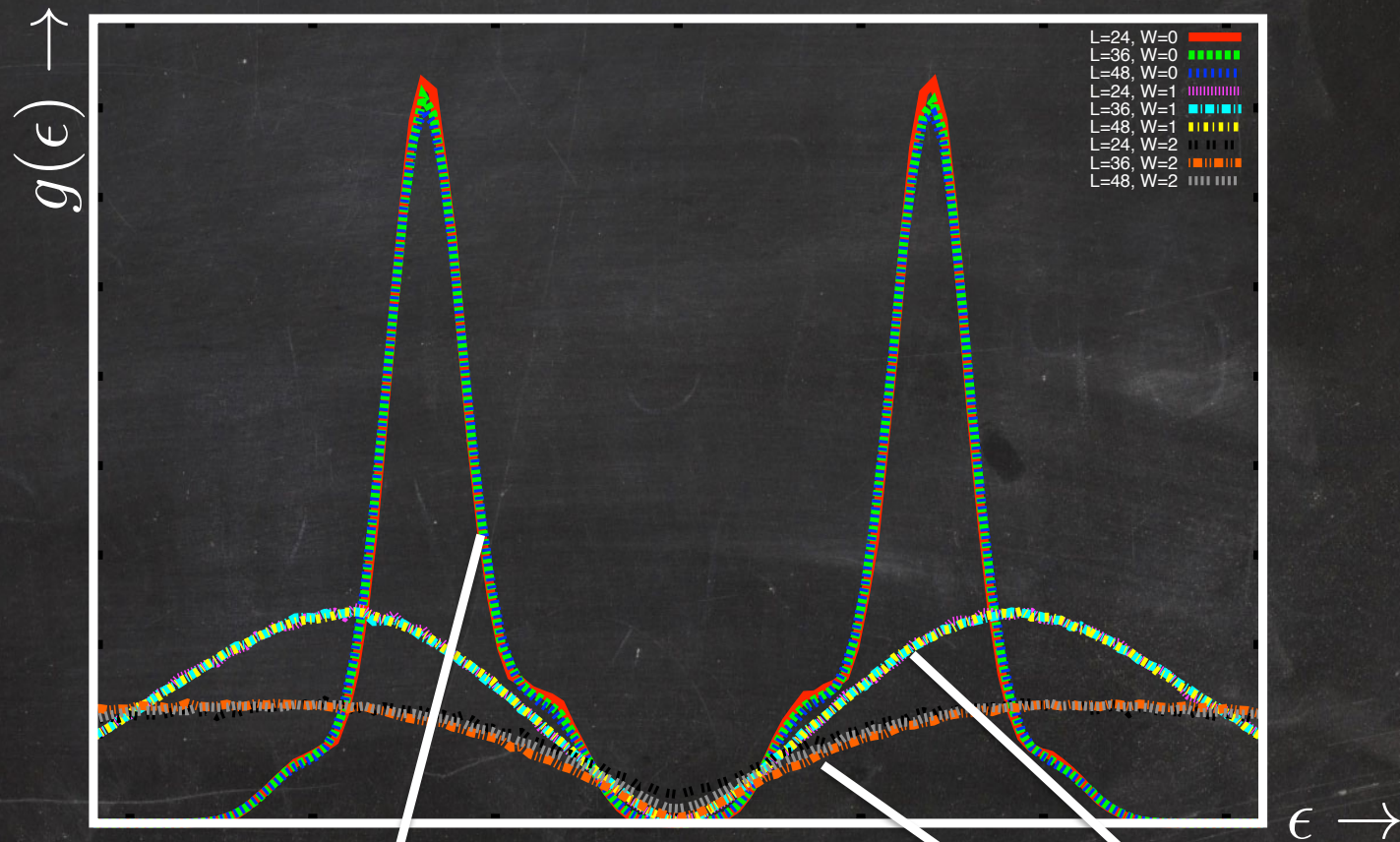


$$H = \frac{1}{2} \sum_{ij} \frac{V}{|r_{ij}|} (n_i - \bar{n}) (n_j - \bar{n})$$

Numerically:

Rapid **quench** to get
metastable state

Coulomb gap without disorder!



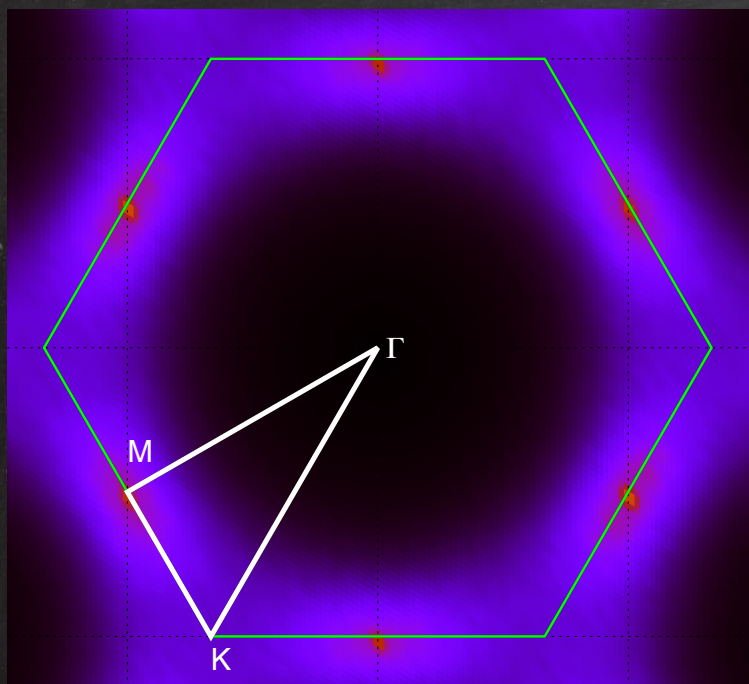
Stronger Coulomb gap
in absence of disorder!

$$g(\epsilon) \sim e^{-\Delta/|\epsilon|}$$

Linear ES gap
with disorder

Why stronger gap?

Metastable states have **local charge correlations**



Restricts the available sites
hence lower d.o.s.

Analytical expression

$$g(\epsilon) \sim |\epsilon|^{-2} e^{-V/\xi|\epsilon|}$$

Conclusions & Thanks!

Disorder-free supercool 😎 electron glass displays
stronger Coulomb gap

Metastable states in disorderfree electron glass
are strongly charge-correlated

Reference: Mahmoudian, Rademaker, et. al., arXiv:1412.4441 on disorder-free glasses; gapwork to be published.

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